luamesh

compute and draw meshes with LuaLaTeX

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https://plmlab.math.cnrs.fr/mchupin/luamesh

luamesh: compute and draw meshes with LuaLATEX

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The package luamesh allows to compute and draw 2D Delaunay triangulation. The algorithm is written with lua, and depending on the choice of the "engine", the drawing is done by MetaPost (with luamplib) or by tikz.

The Delaunay triangulation algorithm is the Bowyer and Watson algorithm. Several macros are provided to draw the global mesh, the set of points, or a particular step of the algorithm.

I would like to thank Jean-Michel Sarlat, who hosts the development with a git project on the melusine machine:

https://melusine.eu.org/syracuse/G/delaunay/

I would also like to thank the first user, an intensive *test* user, and a very kind English corrector: Nicole Spillane.

Contents

1 Installation

`luamesh` is on the CTAN and can be installed with the package manager of your distribution.

<div align="center">

https://www.ctan.org/pkg/luamesh

</div>

Of course, you can just put the two files `luamesh.lua` and `luamesh.sty` in the working directory but this is not recommended.

1.1 With TEXlive and Linux or Mac OSX

To install `luamesh` with TEXlive, you have to create the local `texmf` directory in your `home`.

```
user $> mkdir ~/texmf
```

Then place the files in the correct directories. The `luamesh.sty` file must be in directory:

<div align="center">

~/texmf/tex/latex/luamesh/

</div>

and the `luamesh.lua`, the `luamesh-tex.lua` and the `luamesh`polygon.lua+ files must be in directory:

Once you have done this, `luamesh` can be included in your document with

```
\usepackage{luamesh}
```

1.2 With MikTEX and Windows

As these two systems are unknown to the contributor, we refer to the documentation for integrating local additions to MikTEX:

http://docs.miktex.org/manual/localadditions.html

1.3 A LuaLATEX package

If you want to use this package, you must compile your document with `lualatex`:

```
user $>    lualatex mylatexfile.tex
```

1.4 Dependencies

This package is built upon two main existing packages that one used to draw the triangulations :

1. `luamplib` to use MetaPost via the LuaTEX library `mplib`;

2. `tikz`.

We will see how to choose between these two *drawing engines*. Moreover, the following packages are necessary:

1. `xkeyval` to manage the optional arguments;

2. `xcolor` to use colors (required by `luamplib`);

3. `ifthen` to help programming with TEX.

2 The Basic Macros

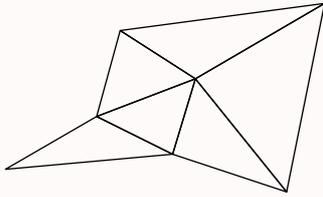This package provides macros to draw two dimensional triangulations (or meshes).

2.1 Draw a Complete Mesh

\buildMeshBW[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}

This macro produces the Delaunay triangulation (using the Bowyer and Watson algorithm) of the given ⟨*list of points*⟩. The list of points must be given in the following way :

```
(x1,y1);(x2,y2);(x3,y3);...;(xn,yn)
```

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```
\buildMeshBW{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}
```


2.1.1 The Options

There are several options to customize the drawing.

`mode = int (default)` **or** `ext:` this option allows to use either the previously described set of points in the argument, or a file containing the points line by line (in 2 columns). Such a file looks like :

```
x1  y1
x2  y2
x3  y3
...
xn  yn
```

`bbox = none (default)` **or** `show:` this option allows to draw the points added to form the *bounding box*[1] and the triangles attached. By default, these triangles are removed at the end of the algorithm.

`color = ⟨value⟩ (default: black):` The color of the drawing.

`colorBbox = ⟨value⟩ (default: black):` The color of the drawing for the elements (points and triangles) belonging to the bounding box.

`print = none (default)` **or** `points` **or** `dotpoints:` The `point` value allows to label the vertices of the triangulation. This also adds a *dot* at each vertex. The `dotpoints` value only add a dot without the labeling.

`meshpoint = ⟨value⟩ (default: P):` The letter(s) used to label the vertices of the triangulation. It is included in the math mode delimiters `$...$`. The bounding box points are labeled with numbers 1 to 4 and with a star exponent.

`tikz (boolean, default:false):` By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` becomes the *drawing engine.*

---

[1]The bounding box is defined by four points place at 15% around the box defined by (x_{min}, y_{min}), (x_{min}, y_{max}), (x_{max}, y_{max}), and (x_{min}, y_{max}). It is used by the algorithm and will be computed in any case.

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axes). It must contain the unit of length (cm, pt, etc.).

To illustrate the options, let us show you an example. We consider a file `mesh.txt`:

```
0.3    0.3
1.5    1
4      0
4.5    2.5
1.81   2.14
2.5    0.5
2.8    1.5
```

```
\buildMeshBW[%
tikz,
mode = ext,
bbox = show,
color = red,
colorBbox = blue!30,
print = points,
meshpoint = x,
scale = 1.3cm,
]{mesh.txt}
```
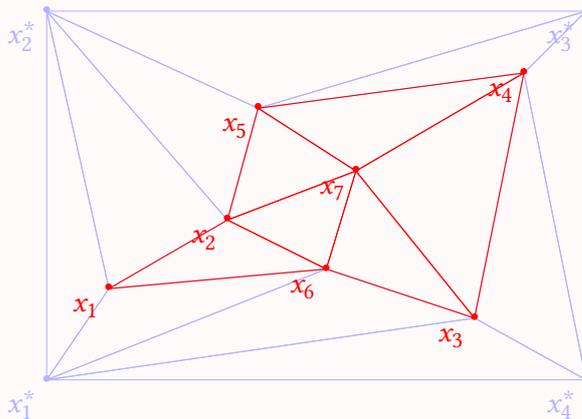

The drawing engine is not very relevant here, although it is useful to understand how the drawing is produced. However, the engine will be relevant to the so called *inc* macros (section 3) for adding code before and after the one generated by `luamesh`.
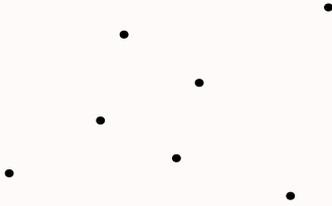
2.2 Draw the Set of Points

\drawPointsMesh[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}

With the `\drawPointsMesh`, we plot the set of (user chosen) points from which the Bowyer and Watson algorithm computes the triangulation.

The use of this macro is quite similar to `\buildMeshBW`. Here is an example of the basic uses.

```
\drawPointsMesh{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}
```

2.2.1 The Options

There are several options (exactly the same as for the `\buildMeshBW`) to customize the drawing.

mode = `int (default)` *or* `ext`: this option allows to use either the previously described set of points as the argument, or a file containing the points line by line (in 2 columns). Such a file looks like :

```
x1  y1
x2  y2
x3  y3
...
xn yn
```

bbox = `none (default)` *or* `show`: this option allows to draw the points added to form the *bounding box*[2] and the triangles attached. By default, these triangles are removed at the end of the algorithm. *Here, because we plot only the vertices of the mesh, there are no triangles, only dots.*

color = ⟨*value*⟩ `(default: black)`: The color of the drawing.

colorBbox = ⟨*value*⟩ `(default: black)`: The color of the drawing for the elements (points and triangles) belonging to the bounding box.

print = `none (default)` *or* `points`: To label the vertices of the triangulation. This also adds a *dot* at each vertex. With no label, the dot remains.

meshpoint = ⟨*value*⟩ `(default: P)`: The letter(s) used to label the vertices of the triangulation. This is included in the math mode delimiters `$...$`. The bounding box points are labeled with numbers 1 to 4 and with a star exponent.

---

[2]The bounding box is defined by four points place at 15% around the box defined by $(x_{\min}, y_{\min})$, $(x_{\min}, y_{\max})$, $(x_{\max}, y_{\max})$, and $(x_{\min}, y_{\max})$. It is used by the algorithm and will be computed in any case.

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tikz (boolean, default:false): By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` becomes the *drawing engine.*

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axes). It must contain the unit of length (cm, pt, etc.).

With the same external mesh point file presented in section 2.1, we illustrate the different options.

```
\drawPointsMesh[%
tikz,
mode = ext,
bbox = show,
color = blue,
colorBbox = red,
print = points,
meshpoint = y,
scale = 1.3cm,
]{mesh.txt}
```
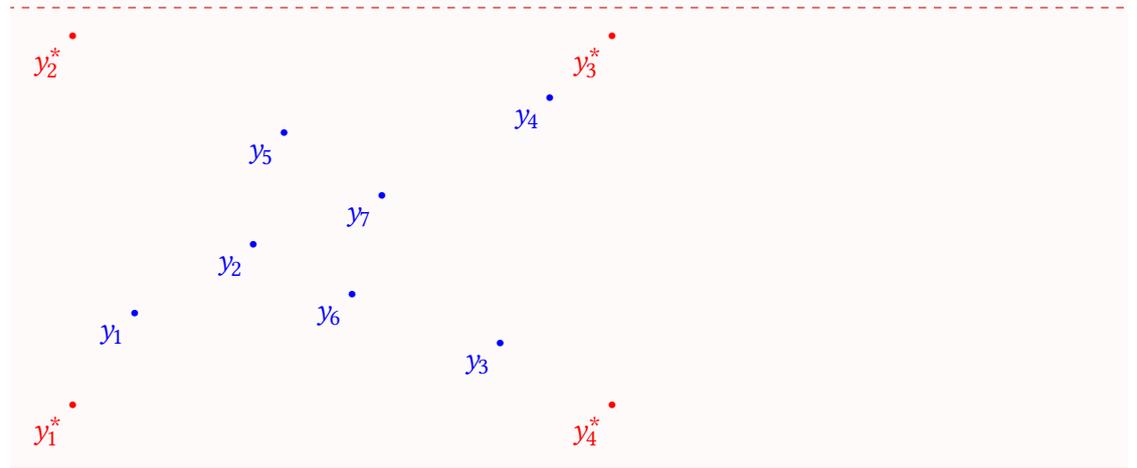

2.3 Draw a Step of the Bowyer and Watson Algorithm

\meshAddPointBW[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}{⟨*point*⟩ or ⟨*number of line*⟩}

This command allows to plot the steps within the addition of a point in a Delaunay triangulation by the Bowyer and Watson algorithm.

This macro produces the Delaunay triangulation (using the Bowyer and Watson algorithm) of the given ⟨*list of points*⟩ and shows a step of the algorithm when the ⟨*point*⟩ is added. The list of points must be given in the following way:
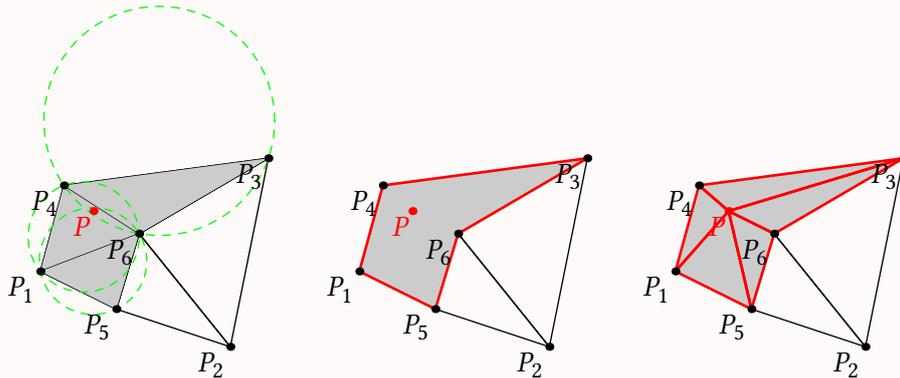
$$(x1,y1);(x2,y2);(x3,y3);...;(xn,yn)$$

and the point is of the form (x,y). The ⟨*file name*⟩ and ⟨*number of line*⟩ will be explained in the option description.

One can use the macro as follows:

```
\meshAddPointBW[step=badtriangles]{(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)
    }{(2.2,1.8)}
\meshAddPointBW[step=cavity]{(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)
    }{(2.2,1.8)}
\meshAddPointBW[step=newtriangles]{(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)
    }{(2.2,1.8)}
```


The default value for `step` is `badtriangles`. Consequently, the first line is equivalent to

```
\meshAddPointBW{(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}{(2.2,1.8)}
```

2.3.1 The Options

There are several options (some of them are the same as for `\buildMeshBW`) to customize the drawing.

`mode = int (default)` **or** `ext:` this option allows to use either the previously described set of points as the argument, or a file containing the points line by line (in 2 columns). Such a file looks like :

```
x1  y1
x2  y2
x3  y3
...
xn  yn
```

For the second argument of the macro, if we are in `mode = ext`, the argument must be the *line number* of the file corresponding to the point we want to add. The algorithm will stop at the previous line to build the initial triangulation and proceed to add the point corresponding to the line requested. The subsequent lines in the file are ignored.

bbox = none (default) *or* show: this option allows to draw the added points that form the *bounding box* and the triangles attached. Although they are always computed, by default, these triangles are removed at the end of the algorithm.

color = ⟨*value*⟩ (default: black): The color of the drawing.

colorBbox = ⟨*value*⟩ (default: black): The color of the drawing for the elements (points and triangles) belonging to the bounding box.

colorNew = ⟨*value*⟩ (default: red): The color of the drawing of the "new" elements which are the point to add, the polygon delimiting the cavity, and the new triangles.

colorBack = ⟨*value*⟩ (default: black!20): The color for the filling of the region concerned by the addition of the new point.

colorCircle = ⟨*value*⟩ (default: green): The color for the circumcircle of the triangles containing the point to add.

meshpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the triangulation. It is included in the math mode delimiters `$...$`. The bounding box points are labeled with numbers 1 to 4 and with a star exponent.

step = badtriangles (default) *or* cavity *or* newtriangles: To choose the step we want to draw, corresponding to the steps of the Bowyer and Watson algorithm.

newpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the new point of the triangulation. It is include in the math mode delimiters `$...$`.

tikz (boolean, default:false): By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` is the *drawing engine*.

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axis). It must contain the unit of length (cm, pt, etc.).

Here is an example of customizing the drawing. First, recall that the external file `mesh.txt` is:

```
0.3    0.3
1.5    1
4      0
4.5    2.5
1.81   2.14
2.5    0.5
2.8    1.5
```
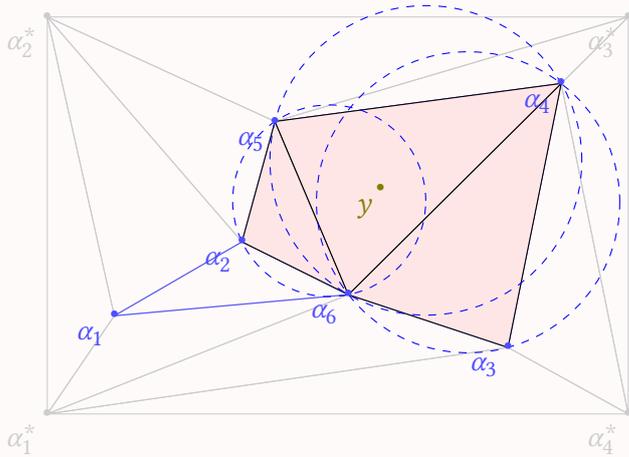
We draw the addition of the 6th point. The 7th line will be ignored.

```
\meshAddPointBW[
tikz,
```

```
mode = ext,
color = blue!70,
meshpoint = \alpha,
newpoint = y,
colorBack=red!10,
colorNew = green!50!red,
colorCircle = blue,
colorBbox = black!20,
bbox = show,
scale=1.4cm,
step=badtriangles]
{mesh.txt}{6}
```


2.4 Mesh a Polygon

\meshPolygon[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}

With `luamesh`, it is possible to mesh an object giving the *border, i.e.,* one closed polygon. The polygon is given as a list of points as above:

$$(x1,y1);(x2,y2);(x3,y3);...;(xn,yn)$$

Once again we can also give a file of points using the `mode` option.

This command allows to plot the steps within the building of a complete mesh. The followed method is, given a parameter h:

- to build a squared grid of points with a unit distance equal to h;

- to keep the grid points inside the polygon;

- if necessary to add points along the polygon to respect the distance parameter;

- to mesh the complete set of points (using the Bowyer and Watson algorithm).

One can use the macro as follows:

```
\meshPolygon[step=polygon,scale=2cm]{(0,0);(1,0);(1,0.5);(0,0.5);(-0.20,0.35);(-0.25,0.25)
    ;(-0.20,0.15)}
\meshPolygon[step=grid,scale=2cm]{(0,0);(1,0);(1,0.5);(0,0.5);(-0.20,0.35);(-0.25,0.25)
    ;(-0.20,0.15)}
\meshPolygon[step=points,scale=2cm]{(0,0);(1,0);(1,0.5);(0,0.5);(-0.20,0.35);(-0.25,0.25)
    ;(-0.20,0.15)}
\meshPolygon[step=mesh,scale=2cm]{(0,0);(1,0);(1,0.5);(0,0.5);(-0.20,0.35);(-0.25,0.25)
    ;(-0.20,0.15)}
```
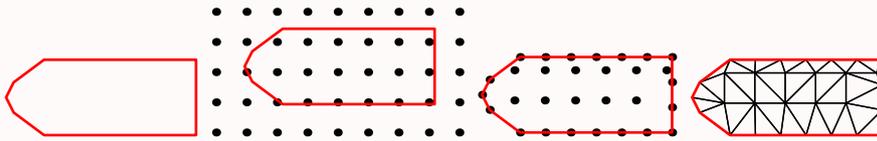

Note that if the points of the grid are too closed to the points of the refined boundary, they are ejected.

2.4.1 The Options

There are several options (some of them are the same as for `\buildMeshBW`) to customize the drawing.

mode = int (default) *or* ext: this option allows to use either the previously described set of points as the argument, or a file containing the points line by line (in 2 columns). Such a file looks like :

```
x1  y1
x2  y2
x3  y3
...
xn  yn
```

h = ⟨*value*⟩ (default: 0.2): The mesh parameter, it is the unit distance for the grid. If necessary, the boundary is refined to get points which respect the distance constrain.

color = ⟨*value*⟩ (default: black): The color of the drawing (the grid point and the mesh).

colorPolygon = ⟨*value*⟩ (default: red): The color of the drawing for the boundary polygon.

print = none (default) *or* points *or* dotpoints: The point value allows to label the vertices of the triangulation. This also adds a *dot* at each vertex. The dotpoints value only add a dot without the labeling.

meshpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the triangulation. It is included in the math mode delimiters `$...$`.

step = polygon *or* grid *or* points *or* mesh (default): To choose the step we want to draw, see the description above.

tikz (boolean, default:false): By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` is the *drawing engine*.

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axis). It must contain the unit of length (cm, pt, etc.).

gridpoints = rect (default) *or* perturb: This option allows to specify the mode of generation of the grid points. The value `rect` produces a simple rectangular grid, and the value `pertub` randomly perturbs the rectangular grid.

Here is an example of customizing the drawing.

```
\meshPolygon[
tikz,
color = blue!70,
meshpoint = \alpha,
colorPolygon=red!100,
scale=4cm,
step=mesh,
print=points,
gridpoints=perturb]
{(0,0);(1,0);(1,0.5);(0,0.5);(-0.20,0.35);(-0.25,0.25);(-0.20,0.15)}
```
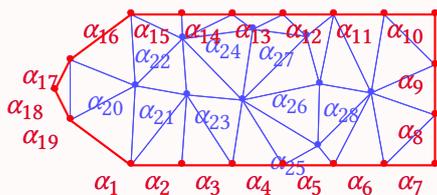

3 The *inc* Macros

The three macros presented in the above sections have complementary macros, with the suffix `inc` that allow the user to add code (MetaPost or `tikz`, depending of the drawing engine) before and after the code generated by `luamesh`.

The three macros are:

\buildMeshBWinc[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}{⟨*code before*⟩}{⟨*code after*⟩}

\drawPointsMeshinc[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}{⟨*code before*⟩}{⟨*code after*⟩}

\meshAddPointBWinc[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}%
{⟨*point*⟩ or ⟨*number of line*⟩}{⟨*code before*⟩}{⟨*code after*⟩}

3.1 With MetaPost

We consider the case where the drawing engine is MetaPost (through the `luamplib` package).

The feature is described for the `\buildMeshBWinc` but the mechanism and possibilities are exactly the same for all three macros.

When we use the MetaPost drawing engine, the macros previously described produce a code of the form

```
\begin{luamplib}
  u:=<scale>;
  beginfig(0);
  <code for the drawing>
  endfig;
\end{luamplib}
```

Then, the arguments ⟨*code before*⟩ and ⟨*code after*⟩ are inserted as follows:

```
\begin{luamplib}
  u:=<scale>;
  <<code before>>
  <code for the drawing>
  <<code after>>
\end{luamplib}
```

> ⓘ With the *inc* macros, the user has to add the `beginfig();` and `endfig;` commands to produce a picture. Indeed, this allows to use the `\everymplib` command from the `\luamplib` package.

3.1.1 The LATEX Colors Inside the MetaPost Code

The configurable colors of the LATEX macro are accessible inside the MetaPost code. For `\buildMeshBWinc` and `\drawPointsMeshinc`, `\luameshmpcolor`, and `\luameshmpcolorBbox` have been defined. For the macro `\meshAddPointBWinc` three additional colors are present: `\luameshmpcolorBack`, `\luameshmpcolorNew`, and `\luameshmpcolorCircle`. For the macro `\meshPolygon`, the color `\luameshmpcolorPoly` is defined. Of course, MetaPost colors can be defined as well. Finally, the `luamplib` mechanism `\mpcolor` is also available.

3.1.2 The Mesh Points

At the beginning of the automatically generated code, a list of MetaPost `pair`s are defined corresponding to all the vertices in the mesh (when the option `bbox=show`, the last 4 points are the *bounding box points*). The points are available with the `MeshPoints[]` table of variables. The `pair`s ($\mathbf{R}^2$ points) `MeshPoints[i]` are defined using the unit length `u`.

With the `\meshPolygon` macro, we have the points of the polygon (refined) that are available with the `polygon[]` table of variables.

3.1.3 Examples

Here is three examples for the different macros.

```
\drawPointsMeshinc[
color = blue!50,
print = points,
meshpoint = x,
scale=0.8cm,
]{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}%
{% code before
  beginfig(0);
}%
{% code after
  label(btex Mesh $\mathbb{T}$ etex, (0,2u)) withcolor \luameshmpcolor;
  endfig;
}
\buildMeshBWinc[%
bbox = show,
color = red,
colorBbox = blue!30,
print = points,
meshpoint = x,
scale=0.8cm
]{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}%
{% code before
  beginfig(0);
}
{% code after
  drawdblarrow MeshPoints[3] -- MeshPoints[9] withpen pencircle scaled 1pt
  withcolor (0.3,0.7,0.2);
  endfig;
}
\meshAddPointBWinc[
meshpoint = \alpha,
newpoint = y,
colorBack=red!10,
colorNew = green!50!red,
colorCircle = blue,
colorBbox = black!20,
bbox = show,
scale=0.8cm,
step=badtriangles]
{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5)}{(2.8,1.5)}%
{%code before
  picture drawing;
  drawing := image(
}{%code after
  );
  beginfig(0);
  fill MeshPoints[7]--MeshPoints[8]--MeshPoints[9]--MeshPoints[10]--cycle
  withcolor \mpcolor{blue!10};
  draw drawing;
```

```
    endfig;
}
```
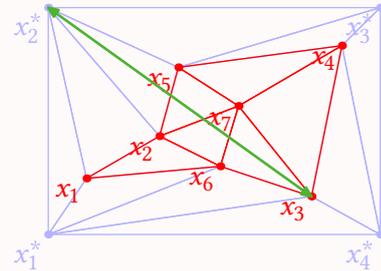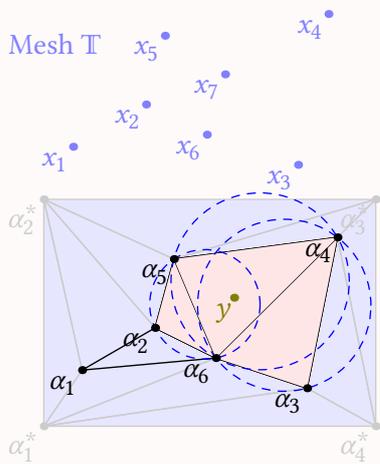

> ℹ The variables `MeshPoints[]` are not defined for the argument corresponding to the code placed **before** the code generated by `luamesh`. Hence, to use such variables, we have to define a `picture` as shown in the third example above.

3.2 With TikZ

If we have chosen `tikz` as the drawing engine, the added code will be written in `tikz`. In that case, the two arguments ⟨*code before*⟩ and ⟨*code after*⟩ will be inserted as follows:

```
\noindent
\begin{tikzpicture}[x=<scale>,y=<scale>]
  <<code before>>
  <generated code>
  <<code after>>
\end{tikzpicture}
```

Because the engine is `tikz` their is no issue with colors, the LaTeX colors (e.g.: `xcolor`) can be used directly.

3.2.1 The Mesh Points

The mesh points are defined here as `tikz \coordinate` and named as follows

```
\coordinate (MeshPoints1) at (...,...);
\coordinate (MeshPoints2) at (...,...);
```

```
\coordinate (MeshPoints3) at (...,...);
%etc.
```

With the `\meshPolygon` we have also the polygon points coordinates:

```
\coordinate (polygon1) at (...,...);
%etc.
```

Once again these coordinates are not yet defined to be used in the code given by ⟨*code before*⟩ argument.

3.2.2 Examples

```
\drawPointsMeshinc[
tikz,
color = blue!50,
print = points,
meshpoint = x,
scale=0.8cm,
]{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}%
{% code before
}%
{% code after
  \node[color = blue!50]  at (0,2) {Mesh $\mathbb{T}$} ;
}
\buildMeshBWinc[%
tikz,
bbox = show,
color = red,
colorBbox = blue!30,
print = points,
meshpoint = x,
scale=0.8cm
]{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5)}%
{% code before
}
{% code after
  \draw[<->,thick, color=green] (MeshPoints3) -- (MeshPoints9);
}
```
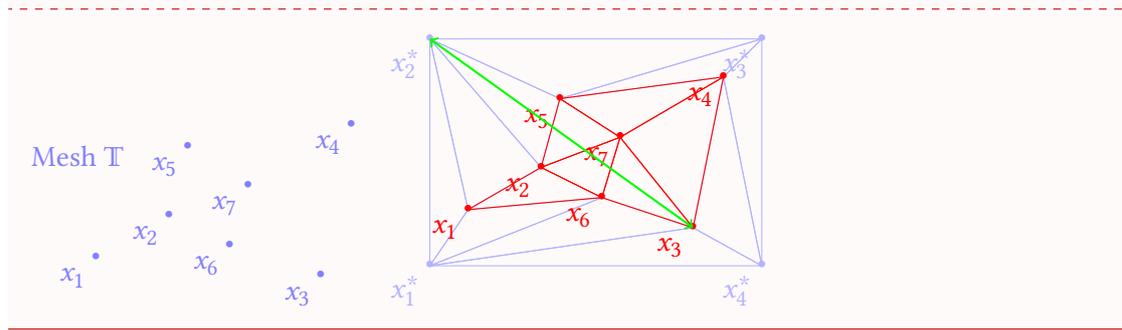
4 Voronoï Diagrams

Another interesting feature of b Delaunay triangulation is that its *dual* is the so-called Voronoï diagram. More precisely, for a finite set of points $\{p_1, \ldots, p_n\}$ in the Euclidean plane, the Voronoï cell R_k corresponding to p_k is the set of all points in the Euclidean plane $\mathbf{R}^2$ whose distance to p_k is less than or equal to its distance to any other $p_{k'}$.

\buildVoronoiBW[⟨*options*⟩]{⟨*list of points*⟩ or ⟨*file name*⟩}

This macro produce the Voronoï diagram of the given ⟨*list of points*⟩. Once again, the list of points must be given in the following way :

$$(x1,y1);(x2,y2);(x3,y3);...;(xn,yn)$$

```
\buildVoronoiBW{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5);(0.1,2)
    ;(1.5,-0.3)}
```


4.1 The Options

There are several options to customize the drawing.

mode = int (default) *or* ext: this option allows to use either the previously described set of points in the argument, or a file containing the points line by line (in 2 columns). Such a file looks like :

```
x1  y1
x2  y2
x3  y3
...
xn  yn
```

bbox = none (default) *or* show: this option allows to draw the added points to form a *bounding box*[3] and the corresponding triangulation. By default, these points are removed at the end of the algorithm.

color = ⟨*value*⟩ (default: black): The color of the drawing.

colorBbox = ⟨*value*⟩ (default: black): The color of the drawing for the elements (points and triangles) belonging to the bounding box.

colorVoronoi = ⟨*value*⟩ (default: black): The color of the drawing for the elements (points and polygons) belonging to the Voronoï diagram.

print = none (default) *or* points: To label the vertices in the triangulation. Contrary to the previous macros, where print=none, a *dot* is produced at each vertex of the set of points and at the circumcircle centers which are the nodes of the Voronoï diagram.

meshpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the triangulation. This is included in the math mode delimiters `$...$`. The bounding box points are labelled with numbers 1 to 4 and with a star exponent.

circumpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the Voronoï diagram. This is included in the math mode delimiters `$...$`.

tikz (boolean, default:false): By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` becomes the *drawing engine*.

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axes). It must contain the unit of length (cm, pt, etc.).

delaunay = none (default) *or* show: This option allows to draw the Delaunay triangulation under the Voronoï diagram.

styleDelaunay = none (default) *or* dashed: This option allows to draw the Delaunay triangulation in dashed lines.

styleVoronoi = none (default) *or* dashed: This option allows to draw the Voronoï edges in dashed lines.

---

[3]The bounding box is defined by four points place at 15% around the box defined by (x_{min}, y_{min}), (x_{min}, y_{max}), (x_{max}, y_{max}), and (x_{min}, y_{max}). It is used by the algorithm and will be computed in any case.

```
\buildVoronoiBW[tikz,delaunay=show,styleDelaunay=dashed]
{(0.3,0.3);(1.5,1);(4,0);(4.5,2.5);(1.81,2.14);(2.5,0.5);(2.8,1.5);(0.1,2);(1.5,-0.3)}
```
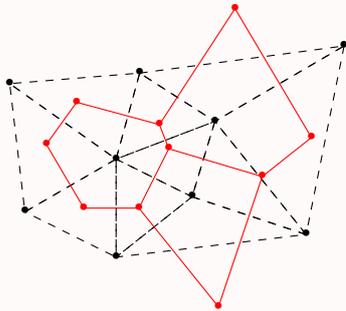

4.2 The *inc* variant

Once again, a variant of the macros is available allowing the user to add code before and after the code produced by `luamesh`. We refer to section 3 because it works the same way.

Let us note that:

- with MetaPost, the circumcenters are defined using `pair CircumPoints[];` and so they are accessible.

- With `tikz`, there are new coordinates defined as follows

```
\coordinate (CircumPoints1) at (...,...);
\coordinate (CircumPoints2) at (...,...);
\coordinate (CircumPoints3) at (...,...);
% etc.
```

Finally, when the MetaPost drawing engine is used another color is available (see 3.1.1): `\luameshmpcolorVoronoi`.

5 With Gmsh

Gmsh is an open source efficient software that produces meshes. The exporting format is the *MSH ASCII file format* and can be easily read by a Lua program. `luamesh` provides the user with dedicated macros to read and draw meshes coming from a Gmsh exportation.
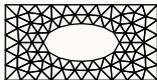
`\drawGmsh[⟨options⟩]{⟨file name⟩}`

This macro draws the triangulation produced by Gmsh and exported in the `msh` format. The argument is the name of the file to be read (e.g.: `maillage.msh`).

Since the version 0.6, `luamesh` support both version 2 and 4 of the *MSH ASCII file format*.

```
\drawGmsh{maillage.msh} % version 2.2 of MSH ASCII file format
```
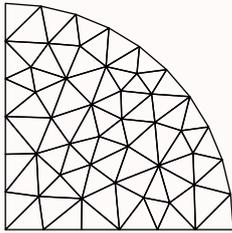


```
  \drawGmsh{maillagev4.msh} % version 4.1 of MSH ASCII file format
```


There are several options to customize the drawing.

color = ⟨*value*⟩ (default: black): The color of the drawing.

print = none (default) *or* points: To label the vertices of the triangulation. Contrary to some previous macros, when print=none a *dot* is produced at each vertex of the set of points and at the circumcircle centers (these are the nodes of the Voronoï diagram).

meshpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the triangulation. This is included in the math mode delimiters $...$. The bounding box points are labeled with numbers 1 to 4 and with a star exponent.

tikz (boolean, default:false): By default, this boolean is set to false, and MetaPost (with luamplib) is used to draw the picture. With this option, tikz becomes the *drawing engine*.

scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axes). It must contain the unit of length (cm, pt, etc.).

Here is an example:

```
  \drawGmsh[scale=2cm,print=points, color=blue!30]{maillage.msh}
```
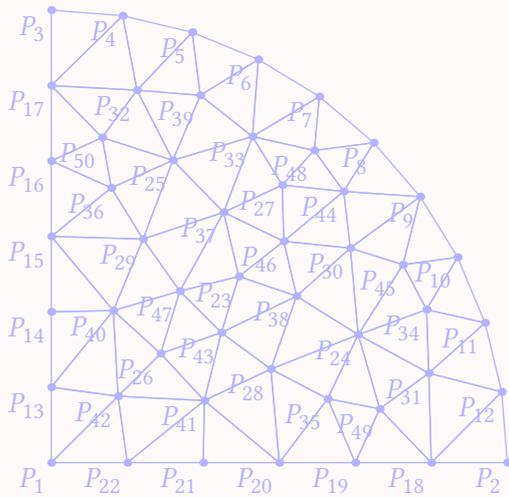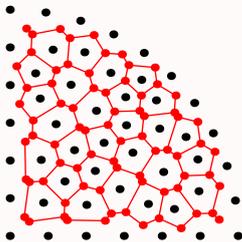
5.1 Gmsh and Voronoï Diagrams

Because Gmsh generates Delaunay triangulations, we can plot the associated Voronoï diagram. This is done by the following macro:

\gmshVoronoi[⟨*options*⟩]{⟨*file name*⟩}

```
\gmshVoronoi{maillage.msh}
```


5.2 The Options

There are several options to customize the drawing.

color = ⟨*value*⟩ (default: black): The color of the drawing.

colorVoronoi = ⟨*value*⟩ (default: black): The color of the drawing for the elements (points and polygons) belonging to the Voronoï diagram.

print = none (default) *or* points: To label the vertices of the triangulation. Contrary to some previous macros, when print=none, a *dot* is produced at each vertex of the set of points and at the circumcircle centers (these are the nodes of the Voronoï diagram).

meshpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the triangulation. It is included in the math mode delimiters `$...$`. The bounding box points are labeled with numbers 1 to 4 and with a star exponent.

circumpoint = ⟨*value*⟩ (default: P): The letter(s) used to label the vertices of the Voronoï diagram. This is included in the math mode delimiters `$...$`.

tikz (boolean, default:false): By default, this boolean is set to `false`, and MetaPost (with `luamplib`) is used to draw the picture. With this option, `tikz` becomes the *drawing engine*.
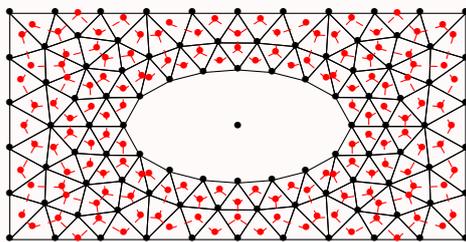
scale = ⟨*value*⟩ (default: 1cm): The scale option defines the scale at which the picture is drawn (the same for both axes). It must contain the unit of length (cm, pt, etc.).

delaunay = none (default) *or* show This option allows to draw the Delaunay triangulation overlapped with the Voronoï diagram.

styleDelaunay = none (default) *or* dashed This option allows to draw the Delaunay triangulation in dashed lines.

styleVoronoi = none (default) *or* dashed This option allows to draw the Voronoï edges in dashed lines.

```
\gmshVoronoi[tikz,scale=3cm, delaunay=show,styleVoronoi=dashed]{maillagev4.msh}
```


5.3 The *inc* variants

Once again, there exist *inc* variant macros:

`\drawGmshinc[⟨options⟩]{⟨file name⟩}{⟨code before⟩}{⟨code after⟩}`

`\gmshVoronoiinc[⟨options⟩]{⟨file name⟩}{⟨code before⟩}{⟨code after⟩}`

We refer to the previous sections for explanations.

6 Gallery

6.1 With Animate

If you use *Adobe Acrobat reader*, you can easily produce an animation of the Bowyer and
Watson algorithm with the package animate.

For example, the following code (in a file name animation.tex):

```
\documentclass{article}
%% lualatex compilation
\usepackage[margin=2.5cm]{geometry}
\usepackage{luamesh}
\usepackage{fontspec}
\usepackage{multido}
\pagestyle{empty}
\def\drawPath{draw (-2,-2)*u--(8,-2)*u--(8,6)*u--(-2,6)*u--cycle  withcolor 0.99white;}
\def\clipPath{clip currentpicture to (-2,-2)*u--(8,-2)*u--(8,6)*u--(-2,6)*u--cycle;}
\begin{document}
\drawPointsMeshinc[mode=ext, bbox = show,colorBbox = blue!20,print=points]{mesh.txt}%
{%
  beginfig(0);
  \drawPath
}%
{%
  \clipPath
  endfig;
}
\newpage\buildMeshBWinc[mode=ext,bbox = show,colorBbox = blue!20,print=points]{meshInit.txt}%
{%
  beginfig(0);
  \drawPath
}%
{%
  \clipPath
  endfig;
}
\multido{\ii=5+1}{4}{%
  \newpage\meshAddPointBWinc[mode=ext,step=badtriangles,colorNew
  =green!20!red,colorBack=red!10,colorCircle = blue,bbox =
  show,colorBbox = blue!20]{mesh.txt}{\ii}%
  {%
    beginfig(0);
    \drawPath
  }%
  {%
    \clipPath
    endfig;
  }    \newpage
  \meshAddPointBWinc[mode=ext,step=cavity,colorNew
  =green!20!red,colorBack=red!10,colorCircle = blue,bbox =
  show,colorBbox = blue!20]{mesh.txt}{\ii}%
  {%
```

```
      beginfig(0);
      \drawPath
    }%
    {%
      \clipPath
      endfig;
    }  \newpage
    \meshAddPointBWinc[mode=ext,step=newtriangles,colorNew
    =green!20!red,colorBack=red!10,colorCircle = blue,bbox =
    show,colorBbox = blue!20]{mesh.txt}{\ii}%
    {%
      beginfig(0);
      \drawPath
    }%
    {%
      \clipPath
      endfig;
    }
  }
  \newpage
  \buildMeshBWinc[mode=ext,bbox = show,colorBbox = blue!20,print=points]{mesh.txt}%
  {%
    beginfig(0);
    \drawPath
  }%
  {%
    \clipPath
    endfig;
  }
  \newpage
  \buildMeshBWinc[mode=ext,print=points]{mesh.txt}%
  {%
    beginfig(0);
    \drawPath
  }%
  {%
    \clipPath
    endfig;
  }
\end{document}
```

produces a PDF with multiple pages. Using the `pdfcrop` program, we crop the pages to the material, and then we can animate the PDF using the `animate` package.

7 History

- June, 6th, 2020, v 0.6, correction of bug produced by the deleted `\mplibcolor` function of `luamplib` package.

- June, 6th, 2020, v 0.6, add support of version 4 of the *MSH ASCII file format*.

References

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